Theories of dark matter

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We have solid evidence for dark matter:



 Ω_{M}



We have solid evidence for dark matter:





Our goal: Understand the properties of dark matter.

This talk

- Going over our basic understanding and main scenarios of dark matter.
- Focusing on theoretical aspects of dark matter models
- It is a HUGE subject.
 - This talk is only an overview and glossing over many details.

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 - ▶ If it decays, lifetime much longer than the age of universe $\approx 10^{17}$ sec.

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 - Does not have electric charge



- Stable.
 - ▶ If it decays, lifetime much longer than the age of universe $\approx 10^{17}$ sec.
- Dark. Does not emit/absorb/reflect light.
 - Does not have electric charge.
- Produced in the early universe with the right amount. Right "relic abundance"



- Seed structures in the universe.

We begin with quantum fluctuations in early universe

$z \simeq 10^7, T \sim 2 \text{ keV}$

- Seed structures in the universe.



Dark matter follow these inhomogeneities

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 keV

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Dark matter follow these inhomogeneities

Dark matter needs to be "primordial", be there in early universe.

$$z\simeq 10^7, T\sim 2 \text{ keV}$$



- "Collisionless". No long range interaction, except gravity.

- Cold. Non-relativistic: kinetic energy \ll mass

DM needs to seed structures

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NGC 0147 2MASS - Dwarf spheroidal galaxy - Wikipedia

Smallest structure DM seeded: Dwarf spheroidal galaxy, size ≈ 1 kpc (3000 lyr)

Dark matter particle wave packet must be smaller, Lightest ⇔ largest de Broglie wave length

$$\lambda_{\rm dB} = \frac{2\pi}{m_{\rm DM}v} \approx 0.4 \,\,\rm kpc \left(\frac{10^{-22} \rm eV}{m_{\rm DM}}\right)$$

NGC147 (left) and the Forn: NGC147) of the Unknown author - Two Micron All Sky Survey (2MASS)

5/26/2021

vikipedia.org/wiki/Dwarf_spheroidal_galaxy#/media/File:N 2265frknown author - Two Microrth All Sky Survey (2MASS)

https://en.wikipedia.org/wiki/Dwarf_spheroidal_galaxy#/media/File:NGC_0147_2MASS.jpg

"Fuzzy dark matter"





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"Fuzzy dark matter"



Upper bound? Large primordial blackholes (PBH) formed in early universe.

10-22 eV

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Very heavy BH accrete matter, too much ionizing radiation, CMB constraints M_{PBH} < 10s M_☉

Blackhole lighter than $10^{-17} M_{\odot}$ will evaporate in the age of universe, not dark.

Other searches...





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> 80 order of magnitudes!

What else can we say?







 $m_{\rm DM} > 10s \text{ eV}$



Warm dark matter limit:

Dark matter needs to be cold (non-relativistic) for the smallest structure it can seed.

For dark matter particle (in thermal equilibrium) m_{DM} > keV (10³ eV)

Could be ways of getting around this if DM is not in thermal eq., or there is some ways they can cool.





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- 2) How is dark matter produced in the early universe?



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Vast number of models, only a few good theories.

Mass of dark matter



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WIMP (weakly interacting massive particle)



Dark matter in thermal equilibrium with the known (Standard Model) particles in the early universe.

Interaction rate faster than the expansion of the universe

WIMP (weakly interacting massive particle)



Dark matter in thermal equilibrium with the known (Standard Model) particles in the early universe.

Dark matter number density predicted by thermal eq: N_{EQ}

WIMP (weakly interacting massive particle)



As universe expands, dark matter become rare. The DM-SM interaction rate can't keep up. DM drops out thermal eq.

Dark matter density become fixed, "Freeze-out"

A simple picture of interaction



To get the correct relic abundance:

 $\langle \sigma v \rangle \approx 2 \times 10^{-26} \mathrm{cm}^3 \mathrm{/s}$

Two limits





Limit on coupling: g < $4\pi \Rightarrow M_{DM}$ < 100s TeV


Two limits



$$m_{\rm DM} < m_V, \quad \sigma v \sim rac{{\sf g}^4}{4\pi} rac{m_{\rm DM}^2}{m_{
m V}^4}$$
g: coupling

 $m_V \, \thickapprox \, 10^2 \, \mbox{ GeV} \, \Rightarrow \, m_{DM}$ > GeV



Simple WIMP model



Mediated by a known interaction:

The weak interaction in the Standard Model

Mediator mass: 10² GeV

DM part of a EW multiplet



- Simplicity: there is no additional new mediator.

- ▶ Mediated by W/Z/h.
- In SUSY, there are two such examples
 - ▶ Higgsino: doublet. Wino: triplet.

More generally.

n: $SU(2)_L$, Y: Hyper charge

Model	
$(\operatorname{color}, n, Y)$	
(1,2,1/2)	Dirac
(1,3,0)	Majorana
$(1,3,\epsilon)$	Dirac
(1,5,0)	Majorana
$(1,5,\epsilon)$	Dirac
(1,7,0)	Majorana
$(1,7,\epsilon)$	Dirac

Fermionic dark matter:

Renormalizable interaction completely determined by SM gate interactions.

Very predictive: abundance only depends on the mass of the DM

 M_{DM} with the right DM abundance = Thermal target

More generally.



Bottaro, 2nd muon collider physics potential meeting

WIMP "miracle"



- If $g_D \sim 0.1~M_D \sim 10s~GeV$ TeV
 - ▶ We get the right relic abundance of dark matter.
- Coincide with our expectation for weak(±) scale new physics!

Why is WIMP a good theory?



Reasonable:

Early universe (hot) is in thermal equilibrium. Don't need to know too much detail beyond (before) that.

Can be linked to other motivations for electroweak scale new physics.

Present in many models: SUSY, extra dimension...

Testable:

With a sizable coupling to the known (SM) particle, WIMP can be searched in labs.

Looking around the lamppost





Direct detection



At colliders

5/26/2021

CMS-PAS-SUS-19-012_Figure_023.png (3151×2262)



At colliders Signal of mono-jet, mono-photon...



y 19, 14

Still a lot to be done



Search at future colliders



100 TeV pp collider is needed to cover the EW doublet (Higgsino) and triplet (wino) DM.

Not enough to cover the higher dim multiplets.

Reach at muon collider



With inclusive signal: $E_{CM} \approx 14$ TeV enough to cover n≤3 multiplets.

Higher energy needed to cover higher multiplets (almost reaching $m_{\chi} \approx 1/2 E_{CM}$).

With disappearing track: potential to reach almost $m_{\chi} \approx 1/2 E_{CM}$

Beyond WIMP





Beyond WIMP







Beyond the simple WIMPs



New signals. DM may not be the first dark sector discovery.

Extend the WIMP story to lower masses





 $m_V \approx 10^2 \text{ GeV} \Rightarrow m_{DM} > \text{GeV}$

We should consider lighter mediators, m_V < GeV

Dark photon



dark photon: a quantum superposition of γ and γ'

$$|\gamma_{\text{dark}}\rangle = |\gamma'\rangle + \chi |\gamma\rangle$$

Mediates an interaction with strength $\propto \chi$

Roles of dark photon

As mediator for thermal freeze out. (Discussed earlier)

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Freeze-in





Weak coupling, dark matter not in thermal eq.

It approaches the correct relic abundance.

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Examples

Thermal freeze out: $m_{\rm DM} = 10$ MeV, $m_V = 30$ MeV, $\chi \simeq 10^{-4}$ Freeze in: $m_{\rm DM} = 1$ MeV, $m_V = 10^{-12}$ eV, $\chi \simeq 10^{-6}$

Windows into dark sector: portals

 Any known (SM) particle can in principle have small couplings to dark matter/dark sector.



Higgs/Z factories, such as CEPC Neutrino facilities, fixed target experiments...

Higgs/Z factories.



Jia Liu, Xiaoping Wang, Wei Xue, LTW

Neutrino portal example: HNL



 $\mathcal{L}\supset (HL)N+h\,.\,c\,.$



Theories of dark matter



Dark matter = classical wave

$$n_{\text{occupation}} \simeq \frac{\rho_{\text{DM}}}{M_{\text{DM}}} \times \lambda_{dB}^3 = 10^{94} \left(\frac{10^{-22} \text{eV}}{M_{\text{DM}}}\right)^4$$
$$\lambda_{dB} \sim \text{kpc} \left(\frac{10^{-22} \text{eV}}{M_{\text{DM}}}\right) \quad \rho_{\text{DM}} \simeq 0.4 \text{ GeV/cm}^3$$

- Huge occupation number within a de Broglie wavelength.
 - \triangleright Collective motion \rightarrow classical waves, not a single particle
 - similar to sound, waves on the ocean, traveling on a string...

Classical field in expanding universe



Classical field in two limits

 $H > m_{\phi} \quad \ddot{\phi} + 3H\dot{\phi} + V(\phi) = 0$

Hubble expansion more important

 $H < m_{\phi} \quad \ddot{\phi} + 3H\dot{\phi} + V(\phi) = 0$

mass more important



 $\phi(t) \propto \frac{1}{a^{3/2}(t)} \sin(m_{\phi}t + \phi_0)$

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 $\phi(t) \propto \frac{1}{a^{3/2}(t)} \sin(m_{\phi}t + \phi_0)$

$$\rho \propto m_{\phi}^2 \phi^2(t) \propto \frac{1}{a^3(t)}$$

On large scales, behave same as particle-like matter.

Will similarly cluster, form structure, etc.

Why is axion light?

Potential of a symmetry breaking



A very common phenomenon:
1) Standard Model electroweak
symmetry breaking. Strong interaction.
2) Condensed matter system: phonon,
magnets, BCS...

Excitation in θ direction massless. "Goldstone" boson.

Symmetry $\theta \rightarrow \theta + c \Rightarrow \theta$ is massless.

Small mass can then be generated by a small coupling.

Production: misalignment

 $H > m_{\phi}$

Hubble expansion more important



 $H < m_{\phi}$

mass more important



Need large initial value Possible during inflation.

"The axion" and ALP

QCD (strong interaction) axion: the axion

Axion from breaking of a U(1) PQ global symmetry. Axion mass generated by small non-perturbative effect of strong interaction.

Motivation: QCD strong CP problem.

The neutron electric dipole moment expected from QCD is wrong by at least 9 orders of magnitude.

Axion gives a dynamical solution to this problem.

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Axion like particles: ALPs

Similar light scalar particles.

The property is not dictated by the strong interaction. More general scenarios than the QCD axion.

Axion coupling to the known particles

Main detection channel relies on axion photon coupling


Dark photon dark matter

Multiple production mechanisms:



Similar to Hawking radiation, but applied to expanding universe.



From topological defects (such as cosmic strings) radiation

+ from misalignment, coupling to axions, ...



Dark photon searches



Heavier dark photon: Colliders, fixed target experiments

Dark photon searches



Lighter dark photon: Terrestrial/table top detectors, astrophysical, ...

Many new ideas still emerging: e.g. H. An, F. P. Huang, J. Liu, W. Due, 2010.15836

Are axion/dark photon good theories?

- Quite reasonable:
 - Based on well known physics (such as Goldstone boson and symmetry breaking).
 - QCD axion can solve strong CP problem.
- Testable:
 - Simple coupling to the Standard Model. Large possible region of coupling strength.
 - Many new development for new techniques.

Pretty good theories. Good guide for experiments.

Other stories

A special feature on the inflaton potential gives large fluctuations ⇒ primordial blackhole production

Gravitational effect during inflation and reheating can produce (very) heavy particles "WIMP-zillars" (10¹²⁻¹⁵ GeV)



The gaps in our stories



- Still, many orders of magnitudes empty.



- Even more if we also take into account coupling strength

Conclusion

- Understanding dark matter is one of the most pressing questions in physics.
- It is also a very difficult task.
 - Vast range of possibilities, yet we know extremely little.
- After decades of effort, we have several good theories: WIMP + dark sector, axion,...
- Much more is needed to cast a wide net! Huge amount of work left to be done!



Limits from annihilation



Narrowing parameter space.



Arkani-Hamed, Delgado, Giudice, 0601041 Cheung, Hall, Pinner, Ruderman, 1211.4873

Example: Higgs portal $H^{\dagger}H\mathcal{O}_{NP}$

H⁺H lowest dim gauge inv op. Most relevant coupling to SM singlet.



De Simone, Giudice, Strumia, 2014

Fermionic Higgs portal.



Similar story, strong constraint. One may evade direct detection

Dark matter part of weak multiplet



- Mediated by W/Z/h.

- Predictive, no unkown particle as mediator.

SUSY DM signal in the compressed case



SUSY DM signal in the compressed case



- Essentially free of physics background.
- Dominated by p_T mis-measured tracks.
- Very promising reach, much better than mono-jet

WIMP searches at colliders



$$M_{\rm WIMP} \le 1.8 \,\,{\rm TeV} \,\, \left(rac{g^2}{0.3}
ight)$$

WIMP searches at colliders



Difficult searches. In the context of future collider, opportunities of new detector/strategies.



can be part of thermal relic story:



What can dark photon do?



 $o_s r_s$

r

 $V \sim \sqrt{\frac{GM_{<}}{r}} \qquad M_{<} \sim \int \rho r^2 dr$

What can dark photon do?



r



Asymmetric DM

 $n_{\rm B} \sim n_{\rm DM}$

Deplete the symmetric part

Neutrino portal example: HNL



$\mathcal{L} \supset (HL)N + h \cdot c$.

